

# The ifa Package

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**Type** Package

**Title** Independent Factor Analysis

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**Depends** mvtnorm

**Description** The package performs Independent Factor Analysis

**License** GPL version 2.0

**URL** [www2.stat.unibo.it/viroli](http://www2.stat.unibo.it/viroli)

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`ifa.aic`*A function to compute the AIC*

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**Description**

A function to compute the Akaike Information Criterion (AIC) for the fitted IFA model, according to the formula  $-2 \times \log\text{-likelihood} + 2 \times \text{npar}$ , where `npar` represents the number of parameters.

**Usage**

```
ifa.aic(output)
```

**Arguments**

`output` The fitted IFA model object, a list including the log-likelihood and the number of parameters

**Value**

It returns a numeric value with the corresponding AIC.

**Author(s)**

Cinzia Viroli

**References**

Sakamoto, Y., Ishiguro, M., and Kitagawa G. (1986). Akaike Information Criterion Statistics. D. Reidel Publishing Company.

Viroli, C. (2005). Choosing the number of factors in Independent Factor Analysis model, Metodoloski Zvezki, Advances in Methodology and Statistics, Vol. II, N. 2, 219-229. Available at [www2.stat.unibo.it/viroli](http://www2.stat.unibo.it/viroli).

**See Also**

[ifa.bic](#)

**Examples**

```
data(memory)
fit<-ifa.em(memory$x,c(2,2),it=50,eps=0.001)
ifa.aic(fit)
```

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`ifa.bic`*A function to compute the BIC*

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**Description**

A function to compute the Bayesian Information Criterion (BIC), also known as Schwarz's Bayesian criterion (SBC), for the fitted IFA model, according to the formula  $-2 * \log\text{-likelihood} + \text{npar} * \log(\text{nobs})$ , where `npar` represents the number of parameters and `nobs` the number of observations in the fitted model.

**Usage**

```
ifa.bic(output)
```

**Arguments**

`output` The fitted IFA model object, a list including the log-likelihood, the number of observations and the number of parameters.

**Value**

It returns a numeric value with the corresponding BIC.

**Author(s)**

Cinzia Viroli

**References**

Schwarz, G. (1978) Estimating the Dimension of a Model, *Annals of Statistics*, 6, 461-464.

Viroli, C. (2005). Choosing the number of factors in Independent Factor Analysis model, *Metodoloski Zvezki, Advances in Methodology and Statistics*, Vol. II, N. 2, 219-229. Available at [www2.stat.unibo.it/viroli](http://www2.stat.unibo.it/viroli).

**See Also**

[ifa.aic](#)

**Examples**

```
data(memory)
fit<-ifa.em(memory$x,c(2,2),it=50,eps=0.001)
ifa.bic(fit)
```

ifa.em

*Fitting an Independent Factor Analysis model by the EM algorithm***Description**

ifa.em is used to perform Independent Factor Analysis on a matrix of data by the Expectation Maximization algorithm.

**Usage**

```
ifa.em(y, ni, it = 15, eps = 0.001, init = NULL, scaling = TRUE)
```

**Arguments**

y	A data matrix with $n$ rows representing observations and $p$ columns representing variables.
ni	A vector containing the number of mixture components for modeling each factor. The number of factors is equal to the length of this vector.
it	The maximum number of iterations of the EM algorithm. By default it is set to 15.
eps	The lower bound for relative variation of the likelihood. It is used as alternative stopping rule for the EM algorithm: if the relative increment of the likelihood is lower than <code>eps</code> the fitting is stopped. The default is 0.001.
init	A list containing initial values for the factor loading matrix (specified by <code>H</code> ) and the variance matrix of the noise term (specified by <code>psi</code> ). If <code>NULL</code> (default) the algorithm starts from the ordinal factor model solution.
scaling	If <code>TRUE</code> (default) the data are scaled before fitting the IFA model

**Details**

Independent Factor Analysis is a latent variable model with independent and non gaussian factors. The  $p$  observed variables  $x$  are modelled in terms of a smaller set of  $k$  unobserved independent latent variables,  $y$ , and an additive specific term  $u$ :  $x=Hy+u$ , where  $u$  is assumed to be normally distributed with diagonal variance matrix `psi` and the factor loading matrix `H` is also termed as *mixing matrix*. The density of each factor is modelled by a mixture of gaussians. The model is fitted by the EM algorithm. The algorithm can be computationally slow in the complex cases.

**Value**

A list containing the components:

H	The estimated factor loading matrix
lik	The log-likelihood computed at each iteration of the EM algorithm
w	A matrix with the estimated weights of the mixtures. Each row contains the weights of each factor

<code>mu</code>	A matrix with the estimated component means of the mixtures. Each row contains the vector means for each factor
<code>vu</code>	A matrix with the estimated component variances of the mixtures. Each row contains the vector variances for each factor
<code>psi</code>	The noise diagonal variance matrix
<code>ni</code>	The input vector specifying the number of components for each mixture
<code>L</code>	The number of factors
<code>numvar</code>	The number of observed variables
<code>numobs</code>	The number of observations
<code>scaling</code>	A logical variable indicating if data have been scaled before performing the EM algorithm
<code>std.err</code>	A list containing standard errors of the EM estimates
<code>init</code>	A list containing the initial values (if specified) of the EM algorithm

### Author(s)

Cinzia Viroli

### References

Attias H. (1999), Independent Factor Analysis, *Neural Computation*, 11, 803–851.

Montanari A., Calo', D.G., Viroli C. (2005), Independent Factor Discriminant Analysis, *Proceedings of Applied Stochastic Models and Data Analysis*, Brest, France, 569-576. Available at [www2.stat.unibo.it/viroli](http://www2.stat.unibo.it/viroli).

### See Also

[ifa.init.random](#), [ifa.init.pca](#)

### Examples

```
data(memory)
init.values<-ifa.init.random(memory$x,2)
fit<-ifa.em(memory$x,c(2,2),it=50,eps=0.0001,init.values)

fit<-ifa.em(memory$x,c(2,2),it=50,eps=0.0001)
plot(ifa.predict(scale(memory$x),fit))
```

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<code>ifa.init.pca</code>	<i>Internal function to initialize the IFA parameters to ordinary factor solution</i>
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### Description

An internal function to initialize the IFA parameters to ordinary factor solution. This is not to be called by the user, since it is automatically called by the function `ifa.em` if the option `init` is `NULL` (default).

### See Also

[ifa.em](#), [ifa.init.random](#)

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<code>ifa.init.random</code>	<i>A function to randomly initialize the IFA parameters</i>
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### Description

A function to initialize the IFA parameters to random values.

### Usage

```
ifa.init.random(y, L)
```

### Arguments

<code>y</code>	The data to be fitted
<code>L</code>	The number of factors

### Value

A list containing 2 initialized parameters:

<code>H</code>	The factor loading matrix
<code>psi</code>	The noise diagonal variance matrix

### See Also

[ifa.init.pca](#)

### Examples

```
data(memory)
init.values<-ifa.init.random(memory$x, 2)
fit<-ifa.em(memory$x, c(2, 2), it=50, eps=0.0001, init.values)
```

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`ifa.predict`*A function to predict the latent variables*

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**Description**

A function to compute the reconstructed factors.

**Usage**

```
ifa.predict(y, output, method = "lms")
```

**Arguments**

<code>y</code>	The data matrix for which factor reconstructions are desired
<code>output</code>	The result of a call to ifa.em
<code>method</code>	The method for reconstructing the factors

**Details**

The function reconstructs the factor scores by different methods: "bartlett", "thompson" or "lms" (least mean squares). The default is "lms".

**Value**

A matrix with factors in columns.

**Author(s)**

Cinzia Viroli

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`memory`*Memory Tests on Alzheimer and Depressed Patients*

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**Description**

Data from study by Robert Hart, concerning ability of memory tests to distinguish between patients with mild Alzheimer's disease, depression, and controls.

**Usage**

```
data(memory)
```

**Format**

memory is a list of 2 components:  $\$y$  is the group variable (1=Alzheimer; 2=Depressed; 3=Normal) and  $\$x$  is a data.frame containing 45 obs. of 6 variables:

HIR : HI Imagery Recall

LIR : LO Imagery Recall

HIUM: HI Imagery Unreminded Memory

LIUM: LO Imagery Unreminded Memory

SM : Storage

RM : Recognition Memory

**References**

Hart, R.P., Kwentus, J.A., Taylor, J.R., & Hamer, R.M. (1988), Productive naming and memory in depression and Alzheimer's type dementia, *Archives of Clinical Neuropsychology*, 3, 313-322.

**Examples**

```
data(memory)
```

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